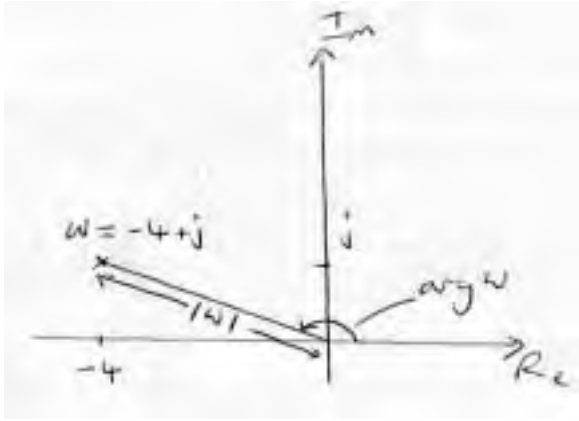
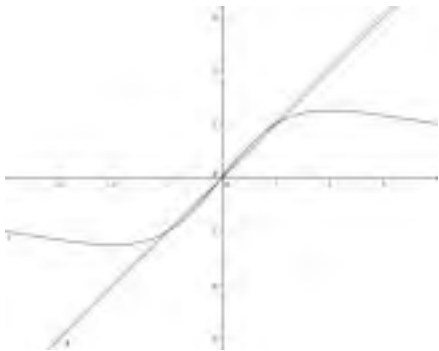
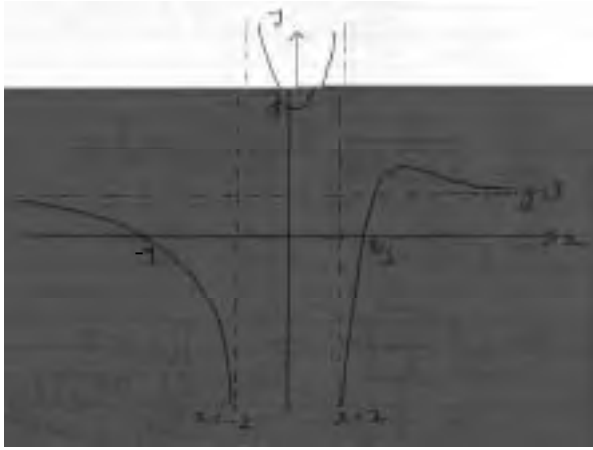
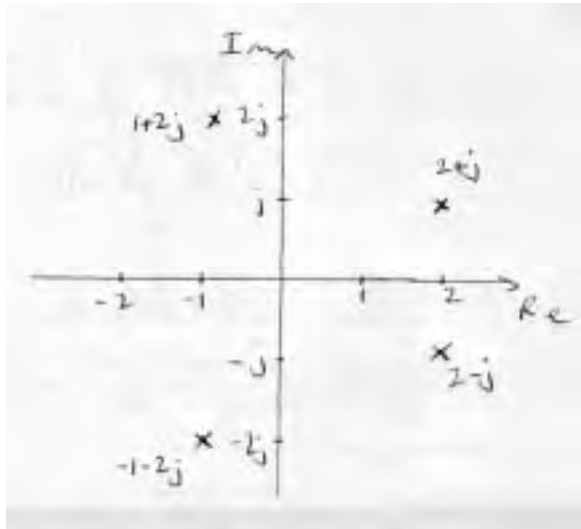


Qu	Answer	Mark	Comment
Section A			
1(i)	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	B1	Accept expressions in sin and cos
1(ii)	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	B1	
1(iii)	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	M1 A1ft	Ans (ii) x Ans (i) attempt evaluation
1(iv)	Reflection in the x axis	B1	
		[5]	
2(i)	$\frac{z+w}{w} = \frac{-1-j}{-4+j} \times \frac{-4-j}{-4-j}$ $= \frac{3+5j}{17} = \frac{3}{17} + \frac{5}{17}j$	M1 A1 A1 [3]	Multiply top and bottom by $-4 - j$ Denominator = 17 Correct numerators
2(ii)	$ w = \sqrt{17}$ $\arg w = \pi - \arctan \frac{1}{4} = 2.90$ $w = \sqrt{17}(\cos 2.90 + j \sin 2.90)$	B1 B1 B1 [3]	Not degrees c.a.o. Accept $(\sqrt{17}, 2.90)$ Accept 166 degrees
2(iii)		B1 B1 [2]	Correct position Mod w and Arg w correctly shown
3	$\alpha + \beta + \gamma = 4 = -p$ $p = -4$ $(\alpha + \beta + \gamma)^2 = \alpha^2 + \beta^2 + \gamma^2 + 2(\alpha\beta + \alpha\gamma + \beta\gamma)$ $\Rightarrow 16 = 6 + 2q$ $\Rightarrow q = 5$	M1 A1 M1 A1 A1 [5]	May be implied Attempt to use $(\alpha + \beta + \gamma)^2$ o.e. Correct c.a.o.

<p>4</p> $\frac{5x}{x^2+4} < x$ $\Rightarrow 5x < x^3 + 4x$ $\Rightarrow 0 < x^3 - x$ $\Rightarrow 0 < x(x+1)(x-1)$ $\Rightarrow x > 1, -1 < x < 0$ 		<p>M1*</p> <p>A1</p> <p>A1</p> <p>M1dep*</p> <p>A1</p> <p>A1</p> <p>[6]</p>	<p>Method attempted towards factorisation to find critical values</p> <p>$x = 0$</p> <p>$x = 1, x = -1$</p> <p>Valid method leading to required intervals, graphical or algebraic</p> <p>$x > 1$</p> <p>$-1 < x < 0$</p> <p>SC B2 No valid working seen</p> <p>$x > 1$</p> <p>$-1 < x < 0$</p>
<p>5</p> $\sum_{r=1}^{20} \frac{1}{(3r-1)(3r+2)} \equiv \frac{1}{3} \sum_{r=1}^{20} \left[\frac{1}{3r-1} - \frac{1}{3r+2} \right]$ $= \frac{1}{3} \left[\left(\frac{1}{2} - \frac{1}{5} \right) + \left(\frac{1}{5} - \frac{1}{8} \right) + \dots + \left(\frac{1}{59} - \frac{1}{62} \right) \right]$ $= \frac{1}{3} \left(\frac{1}{2} - \frac{1}{62} \right) = \frac{5}{31}$		<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>[5]</p>	<p>Attempt to use identity – may be implied</p> <p>Correct use of 1/3 seen</p> <p>Terms in full (at least first and last)</p> <p>Attempt at cancelling</p> <p>c.a.o.</p>

<p>6</p> <p>When $n = 1$, $\frac{1}{4}n^2(n+1)^2 = 1$, so true for $n = 1$</p> <p>Assume true for $n = k$</p> $\sum_{r=1}^k r^3 = \frac{1}{4}k^2(k+1)^2$ $\Rightarrow \sum_{r=1}^{k+1} r^3 = \frac{1}{4}k^2(k+1)^2 + (k+1)^3$ $= \frac{1}{4}(k+1)^2[k^2 + 4(k+1)]$ $= \frac{1}{4}(k+1)^2[k^2 + 4k + 4]$ $= \frac{1}{4}(k+1)^2(k+2)^2$ $= \frac{1}{4}(k+1)^2((k+1)+1)^2$ <p>But this is the given result with $k + 1$ replacing k. Therefore if it is true for k it is true for $k + 1$.</p> <p>Since it is true for $n = 1$, it is true for $n = 1, 2, 3$ and so true for all positive integers.</p>	<p>B1</p> <p>E1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>E1</p> <p>E1</p> <p>[7]</p>	<p>Assume true for k</p> <p>Add $(k+1)$th term to both sides</p> <p>Factor of $\frac{1}{4}(k+1)^2$</p> <p>c.a.o. with correct simplification</p> <p>Dependent on A1 and previous E1</p> <p>Dependent on B1 and previous E1 and correct presentation</p>
Section A Total: 36		

Section B			
7(i)	$(0, 18)$ $(-9, 0), \left(\frac{8}{3}, 0\right)$	B1 B1 B1 [3]	
7(ii)	$x = 2, x = -2$ and $y = 3$	B1 B1 B1 [3]	
7(iii)	Large positive x , $y \rightarrow 3^+$ from above Large negative x , $y \rightarrow 3^-$ from below (e.g. consider $x = 100$, or convincing algebraic argument)	B1 B1 M1 [3]	Must show evidence of working
7(iv)		B1 B1 B1 [3]	3 branches correct Asymptotes correct and labelled Intercepts correct and labelled

<p>8(i)</p> <p>Because a cubic can only have a maximum of two complex roots, which must form a conjugate pair.</p> <p>8(ii)</p> <p>$2 + j, -1 - 2j$</p> <p>$P(z) = (z - (2 - j))(z - (2 + j))(z - (-1 + 2j))(z - (-1 - 2j))$ $= ((z - 2)^2 + 1)((z + 1)^2 + 4)$ $= (z^2 - 4z + 5)(z^2 + 2z + 5)$ $= z^4 - 2z^3 + 2z^2 - 10z + 25$</p> <p>OR</p> <p>$\alpha + \beta + \gamma + \delta = 2 \Rightarrow a = -2$ $\alpha\beta + \alpha\gamma + \alpha\delta + \beta\gamma + \beta\delta + \gamma\delta = 2 \Rightarrow b = 2$ $\alpha\beta\gamma + \alpha\beta\delta + \alpha\gamma\delta + \beta\gamma\delta = 10 \Rightarrow c = -10$ $\alpha\beta\gamma\delta = 25 \Rightarrow d = 25$ $\Rightarrow P(z) = z^4 - 2z^3 + 2z^2 - 10z + 25$</p>		<p>E1 [1]</p> <p>B1 B1</p> <p>M1</p> <p>M1</p> <p>A4</p> <p>M2</p> <p>B1 A3</p>	<p>.</p> <p>Use of factor theorem</p> <p>Attempt to multiply out factors</p> <p>-1 for each incorrect coefficient</p> <p>M1 for attempt to use all 4 root relationships. M2 for all correct $a = -2$ b, c, d correct -1 for each incorrect</p> <p>-1 for $P(z)$ not explicit, following A4 or B1A3</p>
<p>8(iii)</p>	 <p>$z = \sqrt{5}$</p>	<p>[8]</p> <p>B1</p> <p>B1</p> <p>[2]</p>	<p>All correct with annotation on axes or labels</p>

Qu	Answer	Mark	Comment
Section B (continued)			
9(i)	$\mathbf{M} = \begin{pmatrix} 2 & -1 \\ 3 & k \end{pmatrix}$	B2 [2]	- 1 each error
9(ii)	\mathbf{M}^{-1} does not exist for $2k + 3 = 0$	M1	May be implied
	$k = \frac{-3}{2}$	A1	
	$\mathbf{M}^{-1} = \frac{1}{2k+3} \begin{pmatrix} k & 1 \\ -3 & 2 \end{pmatrix}$	B1	Correct inverse
	$\frac{1}{13} \begin{pmatrix} 5 & 1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ 21 \end{pmatrix}$	M1	Attempt to pre-multiply by their inverse
	$= \begin{pmatrix} 2 \\ 3 \end{pmatrix}$	A1ft A1	Correct matrix multiplication c.a.o.
	$\Rightarrow x = 2, y = 3$	A1ft	At least one correct
		[7]	
9(iii)	There are no unique solutions	B1	
		[1]	
9(iv)	(A) Lines intersect (B) Lines parallel (C) Lines coincident	B1 B1 B1 [3]	
			Section B Total: 36
			Total: 72